

Designing an Automated Assessment of Public Speaking Skills Using Multimodal Cues

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ABSTRACT: Traditional assessments of public speaking skills rely on human scoring. We report an initial study on the development of an automated scoring model for public speaking performances using multimodal technologies. Task design, rubric development, and human rating were conducted according to standards in educational assessment. An initial corpus of 17 speakers with four speaking tasks was collected using audio, video, and 3-D motion capturing devices. A scoring model based on basic features in speech content, speech delivery, and hand, body, and head movements significantly predicts human rating, suggesting the feasibility of using multimodal technologies in the assessment of public speaking skills.

Keywords: Automated assessment, multimodal sensing, Kinect, motion tracking, public speaking



1 INTRODUCTION

Oral communication is recognized as one of the most highly valued skills for success in the workplace (cf. Kyllonen, 2012) and school. Public speaking is widely known to be the most feared form of oral communication (Pull, 2012) but is often overlooked in educational assessment. A successful public speaking performance is distributed across multiple modalities — e.g., the speech content, voice and intonation, facial expressions, head poses, hand gestures, and body postures.

While most current rubrics for evaluating public speaking performance attend to both verbal and non-verbal aspects, virtually all existing assessments in practice require human rating (Ward, 2013; Schreiber, Paul, & Shibley, 2012; Carlson & Smith-Howell, 1995). In this article, we describe research using multimodal sensing — namely motion tracking, head tracking, and speech processing — toward developing an assessment system for automated scoring of presentation skills.

The article is organized as follows: Section 2 reviews previous research on a) analyzing presentation performance using oral and multimodal cues and b) multimodal corpora using the Kinect tracking device. Section 3 describes the multimodal presentation corpus we created, including tasks, data recording methods, and the human scoring process. Section 4 describes experiments predicting presentation skills using multimodal features extracted from audio, video, and motion data. Finally, Section 5 summarizes the findings of the paper and discusses future research directions.

2 PREVIOUS RESEARCH

There is an emerging body of literature on using audio and video cues to evaluate presentation skills. In their patent publication, Silverstein and Zhang (2003) depict the use of audio analysis techniques to provide evaluation feedback for real-time oral presentations. Audio alone, however, does not address other modalities of the performance. Rosenberg and Hirschberg (2005) analyzed lexical and prosodic cues for *charisma*, the ability to command authority based on personal qualities. By using a political speech corpus, they found that human raters could rate charisma quite consistently. A set of features, such as F_0 , speaking rate, and the number of first person pronouns, were found useful in predicting charisma. This suggests the possibility of using simple acoustics and lexical cues for predicting paralinguistic related aspects of public speaking.

Scherer, Layher, Kane, Neumann, and Campbell (2012) conducted an audio/visual analysis on a political speech corpus and found some cues related to the rating of speaking performance. Among visual cues, motion energy¹ was found to be correlated with speaking performance. The study also used an eyetracker to analyze subjects' gaze patterns. Kurihara, Goto, Ogata, Matsusaka, and Igarashi (2007)

¹ The details of computing motion energy were provided in Section 3.2 in Scherer, Layher, Kane, Neumann, & Campbell (2012).



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developed a presentation coaching system using Automatic Speech Recognition (ASR), prosody analysis, and image processing. A marker-based computer vision object-tracking method was used for head tracking. However, marker-based and video-only methods for tracking body movements tend to be cumbersome and error-prone.

With the introduction of 3-D sensing devices such as Microsoft Kinect, tracking human movements has become increasingly easy and accurate for multimodal research (Zhang, 2012). Swift et al. (2012) created a multimodal corpus for research on learning everyday tasks, which included audio, video, Kinect RGB-Depth video and object-touch data while subjects demonstrated how to make a cup of tea. Anvil (Kipp, 2012), a very popular video annotation tool, has been updated to include a Kinect recording cookbook and support for displaying Kinect 3-D tracking results.

Kinect devices have been utilized for analyzing speakers' full body behaviours during their presentations. For example, in a brief report, Nguyen, Chen, and Rauterberg (2012) proposed building a public speaking evaluation system. Students participating in a scientific presentation course were recorded using a Kinect device. Body posture and hand gestures were analyzed using Laban Movement Analysis (LMA), a coding scheme widely used in dance analysis. A more comprehensive approach to public speaking performance evaluation is illustrated by Batrinca, Stratou, Shapiro, Morency, and Scherer (2013), who created a public speaking skill training system with a combination of advanced multimodal sensing and virtual human technologies. In particular, MultiSense (Scherer, Stratou, & Morency, 2013) was used to record and recognize a set of the multimodal behaviours of presenters. Meanwhile, a virtual audience would respond to the quality of the presentation in real time to provide feedback and training opportunities. Two Toastmaster club members were asked to rate a set of low-level observations about presentation performance, such as speaking rate, pace, and so on. On such low-level observations, quite high inter-rater agreements were reported.

Recently, a dataset of oral presentations, including slides and corresponding multimodal recordings, was provided in the Multimodal Learning Analytics (MLA) 2014 grand challenge and workshop. This dataset, known as the Oral Presentation Quality Corpus (ESPOL, 2014), was collected in Ecuador as part of a college level course. Students formed groups of up to six people and developed a presentation (in either PowerPoint or PDF format), before delivering their presentations individually. In total, 441 multimodal presentations (approximately 19 hours of multimodal data, i.e., audio, video, and depth data) were recorded using a video camera and a Kinect for Xbox device. The presentations were rated on several dimensions. ESPOL (2014) has released all of the videos, Kinect motion trace files, and associated human scores as part of the MLA 2014 Grand Challenge.

Using this data from the MLA '14 grand challenge, researchers have conducted several initial investigations on the automatic evaluation of the quality of presentations and slides. A summary of these studies can be found in Ochoa, Worsley, Chiluiza, and Luz (2014). In particular, Luzardo, Guamn, Chiluiza, Castells, and Ochoa (2014) investigated using audio cues — i.e., the speaking rate, as estimated



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from audio files, and some basic prosodic analysis — to judge delivery performance. Echeverría, Avendaño, Chiluiza, Vásquez, and Ochoa (2014) investigated using Kinect motion traces for measuring body language performance during presentations. Chen, Leong, Feng, and Lee (2014) used a combination of speech, motion, and head tracking features to predict presentation scores. They first reduced the 9-dimension human scores using the Principal Component Analysis (PCA), resulting in two principal components (PCs) — one for presentation delivery and another for the quality of the slides. Chen, Leong, et al. (2014) demonstrated that a scoring model based on automatically extracted multimodal features can significantly predict human scores in both principal components.

Although the OPQC corpus contains 441 multimodal presentations, it has several drawbacks with its recording setup and human scoring. For example, since the data were collected from real classrooms, sometimes there were issues with noticeable device shaking and the synchronization between video and motion traces. As for human scoring, discrete score bands were not utilized, and there was no double-scoring effort. Finally, the data were exclusively open to the participants of the MLA '14 challenge.

Chen, Feng, et al. (2014) is a preliminary study in this direction. Similar to Batrinca et al. (2013) and ESPOL (2014), a public speaking corpus has been created using a Kinect device for Microsoft to record speakers' full body movements. Based on the motion traces tracked by Kinect, several velocity -related motion features were extracted for inferring speakers' performance. Chen, Feng, et al. (2014) suggested that both speech and visual features play useful roles for automatically predicting presentation human-rated scores.

Two observations can be drawn from the literature. Regarding the technology, a combination of 3-D sensors such as Kinect and high quality audio/video recording has been widely used for evaluating presentation performances. Regarding applications, there is much interest in designing interactive systems for training presentation skills. We believe that multimodal technology can transform traditional human-scored public speaking assessments (Schreiber et al., 2012) and make them more reliable and cost-efficient.

Our primary research question, therefore, is whether machine-generated multimodal features can predict human scores in a standardized performance-based public speaking assessment. The aforementioned multimodal research (Nguyen et al., 2012; Batrinca et al., 2013; Ochoa et al., 2014) has so far been based on non-standardized scoring rubrics and human scoring processes, leaving it vulnerable to reliability threats. One contribution of the current research is to bring technologies and techniques developed in learning and training applications to educational assessment, which places more emphasis on the standardization of task design and scoring rubrics (Joe, Kitchen, Chen, & Feng, in press). To this end, we conducted an initial study to design and prototype a public speaking test with the goal of automated multimodal scoring.



3 MULTIMODAL CORPUS

3.1 Tasks

The prototype assessment included five public speaking tasks. Task A was an icebreaker, in which the speaker introduced him- or herself; this task is not analyzed due to the personally identifiable information involved. Tasks B and C were modelled after prepared informational speeches, in which the speaker was given a pre-prepared slide deck and up to 10 minutes to prepare for the presentation. Task B was a business presentation, in which the speaker was to present a financial report. Task C was a simulated teaching task on the topic targeting middle-school students. The other two tasks were persuasive and impromptu speeches. Task D asked speakers to consider a movie that they did not like but nonetheless recommend it to others. Task E asked speakers to consider a place inconvenient to live in and discuss the benefits of living there. No visual aids were provided for Tasks D and E.

3.2 Multimodal Data Collection

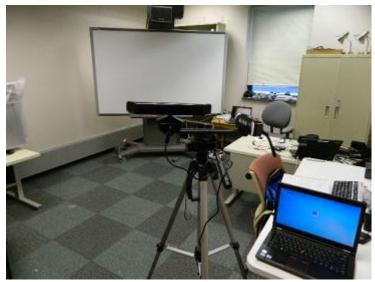
A Microsoft Kinect for Windows Version 1 device was used to record 3-D body motions. Brekel Pro Body Kinect tracking software (v1.3064-bit version) was used to record 48 body joints and stored the motions in the Biovision hierarchical data format (BVH). A JVC Everio GZ-HM35BUSD digital camcorder was used for audio/video recording. The camcorder was mounted together with Kinect on a tripod. The raw vide o resolution used the UXP high definition setting, which uses a 1920x1080i resolution and a bit rate of 24 Mbps on average, and was saved in the MTS format. Note that we did not use wireless microphones that tend to provide clearer recordings compared to the built-in microphone on the camcorder. We made this decision hoping to reduce the complexity of our hardware setup to make the developed technology easier to use in practice. Both the Kinect and the camcorder were placed 6 feet away from the front of the speaking zone, which was marked on the ground. For Tasks B and C, a SMART Board projector system was used to show the PowerPoint slides. Figure 1 shows the apparatus involved in the data collection.

Speakers included 17 volunteers recruited from an education assessment company, with 10 male and 7 female participants. Seven of the participants were experienced public speakers from the Toastmasters Club. The rest varied widely in their public speaking experience. The participants' time was paid for by the employer so they did not receive additional compensation. Before recording, participants completed a 10-item initial background questionnaire related to prior experiences with and attitudes towards public speaking. All participants indicated fluency in English and only two out of the 17 participants reported English as a second or third language. Data from the background questionnaires show that the participants as a whole had prior experience in public speaking: 68.8% of participants estim ated giving professional presentations or prepared talks at least yearly and 37.5% at least monthly.

At the beginning of each structured laboratory recording session, the experimenter reviewed the purpose of the study with the participant and offered an opportunity to have his/her questions



answered. The participant was informed that video, audio, and 3-D motion capture data would be recorded for each of their performances on the five public speaking tasks. After being familiarized with the recording equipment, participants were informed that they were expected to speak for 4 to 5 minutes for Tasks B and C and 2 to 3 minutes for Tasks D and E. To facilitate the pacing of each presentation, participants were signalled by the experimenter first when the minimum required time was reached (4 minutes or 2 minutes) and again when the maximum given time was reached (5 minutes or 3 minutes). Participants were also informed that they would need to make a single audible clap before speaking, with their hands elevated to the torso. The purpose of having participants clap in this way was to allow for an easily distinguishable marker in each of the recording modalities (audio, video,



and motion tracking by Kinect), to help synchronize playback in later analyses.

Figure 1: Apparatus and setting of the data collection. A Microsoft V1 Kinect and a JVC camcorder were mounted together on a tripod. The laptop in the foreground runs the Brekel program for recording motions. The smartboard and the other laptop (away from the readers) were used to present slides for the B and C tasks.

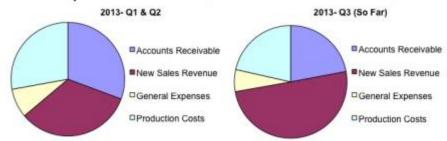
For Tasks B and C, which involved PowerPoint slides, they were given 10 minutes to prepare for their presentation. They were not allowed to have notes during the presentation. Figures 2 and 3 show sample slides from Tasks B and C, respectively.²

For Tasks D and E, the participants were given no preparation time. They would start speaking as soon as they were given the topic of the impromptu speech. Table 1 summarizes the major differences of the se two types of tasks.

² Please contact the correspondence author for task materials.



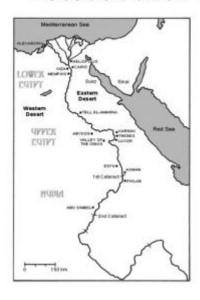
Comparison of Overall Revenue and Expenditures in Quarters 1 and 2 to Q3



- SALES ACCOUNT FOR THE MAJORITY OF REVENUE IN Q3
- Q3 expenses make up a smaller proportion of the total budget

Figure 2: Sample slide from Task B, involving a financial report of a fictitious company.

Location and Features of the Nile



- THE NILE RIVER IS THE LONGEST RIVER IN THE WORLD (6,650 kilometers).
- Ancient Egypt was protected from outside influences, which allowed it to evolve in its own unique way.
- Its flood plain was a magnet for life -- human, plant and animal.

Figure 3: Sample slide from Task C, in which the speaker was asked to give a lecture on the history of ancient Egypt.



Task type	Using	Prep. Time	Speaking	Topics
	Slides	(min)	Time (min)	
Informative	Yes	10	4 to 5	B: business
(B & C)				C: history
Impromptu	No	0	2 to 3	D: movie
(D & E)				E: location

Participants were also given a hand-held USB remote control device for the PowerPoint presentations. Hardcopies of the presentations were available for participants during the preparation stage only. Additional background materials (e.g., further details about historical Egyptian sites) were also provided if the speaker chose to elaborate on certain slides. Speakers were allowed to take notes on scratch paper, but they could not use any of the printed or written notes during the actual presentations. Figure 4 illustrates a speaker emphasizing a point on a slide from Task B.



Figure 4: An illustration of how speakers interacted with the presentation slides during Tasks B and C.

The left panel is a screenshot showing a subject giving the Task B presentation. The face analysis is shown on his face. The right panel shows the motion trace for this video frame.

3.3 Data Processing

After getting raw recordings from our lab sessions, the following steps were taken to process the data for further analysis. The motion and video data streams were synchronized. The HD video files were converted to another format (with a higher compression rate) for playback (e.g., in Xvid or H.263 codec). The audio channel from the video was extracted for several speech processing procedures, including a) manual transcription, b) using the P2FA forced alignment tool (Yuan & Liberman, 2008) to obtain time stamps for all transcribed words (and phonemes), and c) using Praat acoustics analysis software (Boersma & Weeninck, 1996) to extract pitch and intensity measurements. In addition, nonverbal features related to hand movements, body locomotion, and head orientation were computed. More details will be provided in Section 4.1.



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The processed multimodal streams could be imported into Anvil (Kipp, 2012), which supports displaying rich multimodal cues, including playing videos, showing time-aligned transcription, showing audio waveform as well as prosody contours, and other contours, such as hand motion velocity. Therefore, Anvil provides a tool for quickly visualizing this multimodal presentation corpus's content.

3.4 Human Rating

A key emphasis of our research is a reliable, valid, comprehensive assessment of public speaking skills. To this end, we designed a human rating process according to the standard practice in educational assessment. We began with a construct analysis of the skills involved in public speaking and a review of existing assessments and rubrics.

Public speaking is a multifaceted amalgamation of psychological, cognitive, linguistic, and paralinguistic abilities. Assessing public speaking competence is no less complex. Raters process myriad aural and visual behaviours as they evaluate a speaker's public speaking competence. Generally, this process is guided by a scoring rubric that structures the type of behaviours that should be considered and the criteria by which to evaluate those behaviours. One of the challenges of assessing public speaking competence is reliably and accurately detecting the true quality of a performance — filtering the construct-irrelevant factors from the construct-relevant factors.

The final rubric was based on the Public Speaking Competence Rubric (PSCR) (Schreiber et al., 2012) due to its psychometric properties. According to their study, using five trained faculty member raters on 45 speech presentations by college students, the *intraclass correlation coefficients* (ICCs; a measure of variance in scores associated with raters) across the 10 items and holistic scores ranged from .37 to .93, making it one of the most reliable human-scored instruments for assessing public speaking performance. The original PSCR rubric contains 11 items: topic selection, introduction, organization, supporting materials, conclusion, language, vocal expression, non-verbal behaviour, adaptation to audience, visual aids, and persuasiveness. Of the 11 rubric dimensions described above, dimensions 2, 3, and 5–9 were used for the purpose of the present study. The tasks administered did not provide the opportunity for topic selection; the topic was given to the speaker (Dimension 1). Supporting materials were not required (Dimension 4), because there was not enough preparation time given to speakers to gather supporting materials. Dimension 10 was assessed only when the task required use of visual aids (Tasks B and C). Dimension 11 was considered for all tasks even though only two were persuasive in nature. A holistic evaluation component was added to the rubric.

The final scoring rubric adapted from PSCR contains the following items: introduction, organization, conclusion, language, vocal expression, non-verbal behaviour, adaptation to audience, visual aids, and persuasiveness, plus the overall holistic rating. For each item, a five-point Likert score (0 representing the worst performance, 4 representing the best) was used.



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The recruitment and training of human raters is critical for the quality of human scoring. Five raters were recruited from the same educational assessment company. Two expert raters had backgrounds in oral communication/public speaking instruction at the higher education level. The other three (non-expert raters) had extensive experience in scoring essays, but not in scoring public speaking performances. For reliability purposes, all presentations were double-scored. Given the intended use of the human scores for automated scoring development, it was decided that each presentation would receive at least two independent scores. If two scores differed substantially, an adjudication process resolved the discrepancies and resulted in a consensus score.

The scoring process was organized in two phases. Phase 1 involved working with the two expert raters in order to develop criterion scores for a randomly selected subset of presentation videos (12 videos covering the four tasks). The criterion videos and scores were used to train non-expert raters in Phase 2. During the training, non-expert raters reviewed exemplar videos from the criterion set and discussed them with expert raters in order to come to the same scores. The process continued until they could reliably rate the criterion set. This was the first opportunity for raters to use the scoring instrument and provide feedback on its "scorability" (i.e., its usability for the set of tasks and presentations). In Phase 2 expert and non-expert raters worked together to score the remainder of the presentations. Each presentation was randomly assigned to an expert and a non-expert rater, who scored independently.

The final "operational" score is the average of all scores assigned to a given dimension for a given speaker. Experts were randomly paired with non-experts. The expert rater always provided the first score for each presentation. Non-experts were never paired with one another. None of the raters was aware of the type of score (first or second) they were providing. In the event that the scores between two raters were discrepant, a third rater provided an independent score, again without knowledge of the type of score he or she was providing. The third rater assigned scores to all of the dimensions; however, only the scores for the dimensions with two discrepant (R1, R2) scores were used. For details about the scoring and adjudication process, see Joe et al. (in press).

To understand the internal structure of the human scores further, we conducted a principal component analysis (PCA) on all adjudicated sub-scores available in each task type. We were interested in whether there was a common principal component (PC) that could be used as an index of the public speaking performance, and if so, whether it would correlate with the holistic human score. Indeed, we found that the first PC explains 68.8% of variance for the informative tasks and 61.1% of variance for the impromptu tasks. No other PCs had an eigenvalue larger than 1.0. A single factor model is the most parsimonious model for our data. While this conclusion differs from that in Schreiber et al. (2012), which reported a 3-factor model, the empirical results are not inconsistent. Schreiber et al. used an oblique rotation in their factor analysis, which generated three strongly correlated factors. A single factor model may provide comparable fit. In our case, this PC score is highly correlated with the holistic human rating.



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The Pearson correlation r between the holistic scores with the single PC scores is 0.941 for the informative task and 0.93 for the impromptu task.

Some data were lost due to equipment failure. In total, we obtained 56 presentations with complete multimodal recordings. In the experiments described in Section 4, we focused on the final holistic scores after the adjudication process. Regarding holistic scores, between human raters, ICC is 0.385 and Pearson correlation is 0.385 from these 56 videos. Clearly, such ICC values between human raters are quite low. There are many reasons causing such low ICCs. For example, the entire data set was rated through two rounds of ratings; non-expert raters were paired with expert raters in the second round. In addition, compared to the essay/speech scoring task, the video scoring task is still very new and needs more rigorous research on improving the rating reliability.

4 EXPERIMENTS

4.1 Multimodal Features

4.1.1 Textual features

Lexical and syntactic features were extracted using a syntactic complexity analyzer too I on the speech transcripts (Lu, 2010). This is a crude first attempt because speech transcripts differ from written texts in important ways. This tool counts the frequency of 9 types of syntactic structures, e.g., verb phrases (VP), T-units (T), clauses (C), etc., and computes 14 syntactic complexity feature values, such as the mean length of clause (MLC), number of verb phrases per T-unit (VP/T), and number of coordinate phrases divided by number of T-units (CP/T). A complete list of the features can be found in Lu (2010). These features measure syntactic complexity metrics, such as length of production unit, sentence complexity, subordination, coordination, and particular structures.

4.1.2 Speech features

In Batrinca et al. (2013), some basic acoustic and prosodic features were extracted. However, the proposed features relied on human annotation — counting hesitations and filled pauses, and used signal processing that is hard for general users to understand. In this article, we took advantage of recent developments in the automated speech scoring area (Eskenazi, 2009) to obtain effective features that measure speech delivery and other related language skills.

Public speaking skills comprise multiple dimensions, including lexical usage, fluency, pronunciation, prosody, and so on. For example, speaking rate and pause profile have been suggested as useful features in several studies and even in commercial speech-scoring product implementations (Franco et al., 2010; Bernstein, Moere, & Cheng, 2010). A widely used feature for verifying pronunciation is the Goodness of Pronunciation (GOP) tool and its derived features (Witt, 1999; Franco et al., 2010; Chen, Zechner, & Xi, 2009). In particular, following the feature extraction method described in Chen et al.



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(2009), we used speech and transcription to generate a series of features on the multiple dimensions of speaking skills, e.g., speaking rate, prosodic variations, pausing profile, and pronunciation.

4.1.3 Visual features

In previous research on virtual agents, multimodal dialogic systems, and affective computing, a set of methods have been proposed to compute body-language related features for the purpose of either analysis or synthesis. For example, Niewiadomski, Mancini, and Piana (2013) systematically summarized the methods used for analyzing expressive gesture quality. They grouped the features into the three layers: a) low-level features, such as *velocity*; b) medium-level features, such as *repetitive*, *symmetry*; and c) high-level features, such as gestures bearing emotional or social cues. Glowinski et al. (2011) presented a framework for finding a minimal representation of affective gestures, in which head and hand motion data were passed to an array of feature extraction modules, including energy, spatial extent, smoothness, symmetry, head tilt, etc. Then, statistics such as the maximum, mean, and standard deviation (SD) were derived from these basic features. Finally, a minimal set of feature representations was obtained using PCA to reduce dimensionability.

Inspired by this previous research, we extracted a set of low/medium level visual features from Kinect motion traces. We particularly focused on the hip, spine, left forearm, right forearm, left hand, and right hand. Then, the following basic motion features were computed:

- Spatial: for each data frame, a) the distance between the hands and the body (hands-spine); b) the distance between the arms and the body (arms-spine), and c) the distance between the two hands (hands).
- **Temporal**: the first order derivatives of the above spatial measurements; the corresponding features' names contain a special token "1dv." For example, **hands-spine-1dv** indicates the first order derivative of **hands-spine**.
- **Power**: second order derivatives of the above spatial measurements; the corresponding features' names contain a special token "2dv." For example, **hands-spine-2dv** indicates the second order derivative of **hands-spine**.
- **Energy**: Kinetic Energy (*KE*; Niewiadomski et al., 2013) is computed based on the velocities of the upper-body segments and their corresponding percentage of mass. *KE* is computed as

$$KE=0.5 \sum_{i=0}^{n} m_i v_i^2$$



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where m_i is the percentage of mass for the i-th body segment (e.g., left forearm, right hand, and so on) and v_i is the velocity of the i-th segment. Regarding the percentage weight, we used the values in Plagenhoef, Evans, and Abdelnour (1983).³

- **Posture**: Bounding Volume (*BV*), proposed in Niewiadomski et al. (2013), is the normalized volume in a vertical, rectangular, cuboid shape minimally enclosing a speaker's body. *BV* is considered an approximation of the speaker's degree of body "openness."
- **Symmetry**: for each time point *i*, for one axis (*I*) from *X*, *Y*, and *Z*, the symmetry (*SI*) as proposed in Niewiadomski et al. (2013) was computed as

$$SI_{I_i} = \frac{(I_B - I_i^L) - (I_B - I_i^R)}{I_{i_i} - I_{i_i}^L}$$

where I_B is the coordinate of the centre of mass. I_A and I_A are the coordinates of a left joint and corresponding right joint. The average of these symmetry values along the time line is used as the basic feature for each axis. We used two measurements, $SI_{XY} = (SI_X + SI_Y)/2$ and $SI_{XYZ} = (SI_X + SI_Y + SI_Z)/3$.

Then, for each basic feature f, a set of statistics were computed, including

- **mean**: mean value, which is *mean(f)*
- mmrt: ratio of the max value to the mean, which is computed as max(f)/mean(f)
- mean-log: mean of log-scaled value, which is computed as mean(log(f))
- mmrt-log: ratio of max log-scaled value to the mean of log-scaled value, which is computed as max(log(f))/mean(log(f))
- **SD**: standard deviation, which is computed as *SD*(*f*)
- SD-log: standard deviation of log-scaled values, which is computed as SD(log(f))

The orientation of the head approximates the speaker's attention to the audience. Head poses were tracked using the GAVAM head tracker (Morency, Whitehill, & Movellan, 2010) from the video data. Unreliable data (with confidence less than 7.0) were marked as missing. The head features consist of the mean, SD, as well as mean/SD on the log scale, of the horizontal and vertical head movements, which

³ The values can be found from http://www.exrx.net/Kinesiology/Segments.html.



were measured as the angle (in its absolute value) between the head orientation to the zero degree position — the position of squarely facing the camera.

4.2 Feature Selection

The four tasks (B–E) used in our data collection can be grouped into two: Tasks B and C are prepared speeches while Tasks D and E are impromptu speeches. In the first group, the subjects had time to prepare their speeches, used the provided PowerPoint slides to support their speeches, and tended to pace more in front of the Smartboard. In contrast, in the second group, the subjects needed to address the asked questions immediately and had no other resource to refer to. Given these differences in the two kinds of tasks, we anticipated that participants would use verbal and non-verbal cues differently. This speculation was also confirmed by a regression analysis done on our human rated scores. The regression used holistic scores as the independent variable and other dimension scores as dependent variables. Such analysis helps to shed light on the information sources (approximately corresponding to several dimensional scores) used by human raters when making their holistic ratings. Our analysis suggests that different information sources were used for the two task types. For example, the raters gave more weight to non-verbal behaviour and persuasiveness in the impromptu tasks (Tasks D and E). Therefore, we analyzed the results separately for the two groups of tasks, reported in Section 4.3.

Regarding the feature selection, since many features were extracted from different modalities by using different tools, we first ran an unsupervised feature reduction approach to remove one of the features from a pair whose inter-correlation is higher than 0.7. This function is provided by the R caret package (Kuhn, 2008). Next, on the remaining features that are more independent from each other, we selected the features from the speech and body language areas based on their correlation to human judged holistic scores. Since there are only 28 responses for each group, we only picked the features whose correlation magnitude to the final holistic scores was more than 0.38, corresponding to a significant correlation (p<0.05).⁴ Tables 2 and 3 report the selected multimodal features, their corresponding category and brief descriptions, as well as the absolute Pearson correlation values to human judged final holistic scores.

Table 2: A list of multimodal features selected for the prepared speech tasks. Pearson correlations $(|r_{HS}|s)$ between the features and human rated holistic scores are shown in the last column.

Feature	Category	Description	r _{HS}
CP/T	transcript	# coordinate phrases divided by #T-unit	0.515
Silmeandev	fluency	silences' mean deviation	0.570
Ipcount	fluency	# of interruption points (IPs) detected from speech transcript	0.397

⁴ If we had a large data set, such feature selection would be conducted on the training set only.



TOP2	vocab.	freq. of TOP 2 tier words	0.479
TOP5	vobab.	freq. of TOP 5 tier words	0.473
arms-spine-	body	log-scaled mmrt of the 2nd derivative of	0.499
2dv-mmrt-log		the distance between arms and the body	
hands-1dv-	body	the 1st derivative of hands' distance's mean	0.531
mean			
hands-1dv-SD-	- body	1st derivative of hands' distances'	0.441
log		log-scaled SD	

Table 3: A list of multimodal features selected for the impromptu speech tasks. Pearson correlations ($|r_{HS}|$ s) between the features and human rated holistic scores are shown in the last column.

Feature	Category	Description	r _{HS}
Imscore	language-use	language model (LM) score	0.436
wpsec	fluency	speaking rate; words per second	0.462
wdpchk- meandev	fluency	mean deviation of #words among chunks	0.505
withinClause- SilMean	- fluency	mean of the silences within clauses	0.479
face- LeftRight- mean-log	body	face horizontal movement's log-scaled angels' mean	0.387
hands-spine- 1dv-mmrt	body	<i>mmrt</i> of the 1st derivative of the distances between the hands and the body	0.384

Some interesting patterns from the above feature selection result from the two task types. For the prepared speech group, we find that several features measuring speech structure and vocabulary usage were selected, such as *CP/T*, *TOP2*, and *TOP5*. *CP/T* reflected the relative frequency of coordinate phrases in a presentation. Both *TOP2* and *TOP5* features were described in Yoon, Bhat, and Zechner (2012). They measured the frequencies of the spoken words being inside the pre-defined vocabulary sets, such as the *TOP2* and *TOP5* sets. We hypothesized that since a 10-minute preparation time was provided, the speakers had time to refine their speech organization and word choice. Therefore, we found these effective speech features related to language usage for the prepared speech tasks. In addition, another two features, *ipcount* and *withinClause-SilMean*, described in Chen and Yoon (2012), reflect the presentation's organization. Two structural events — i.e., interruption points (IPs) and clause boundaries (CBs) — were automatically tagged and used for computing these structural features. In contrast, the effective speech features found in the impromptu task mostly measure speaking fluency, such as *wpsec*, *wdpchk-meandev*. Possibly such an impromptu task is quite challenging and therefore all participants have a limited performance on high-level linguistic aspects. It is worth noting that the head-orientation feature *face-LeftRight-mean-log* was selected as useful in the impromptu task, which is quite



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consistent with a) our expectations based on the knowledge of non-verbal communication and b) our observations of the videos.

4.3 Predicting Human Holistic Scores

For each task type, i.e., prepared speech vs. impromptu speech, we ran a standard machine learning experiment for using these multimodal features to predict human judged holistic scores. In particular, we ran a leave-one-out cross-validation among all subjects (n=14). In each fold, presentations from 13 subjects were used to train a regression model and then the trained model was applied to the presentations from the remaining subjects. Two regression approaches were utilized, including a) Support Vector Machine (SVM) using a polynomial kernel and b) qlmnet (Friedman, Hastie, & Tibshirani, 2009), two popular models widely used in practical machine learning tasks. Glmnet fits a generalized linear model via penalized maximum likelihood. It provides a very efficient solution to train for the LASSO or elastic net regularized regression model. We used the implementations provided by the R caret package (Kuhn, 2008). Hyper parameters of these machine-learning models were automatically tuned by using a 5-fold cross-validation on the training set. The whole process was repeated 14 times to obtain the machine predicted scores for all of the presentations. Three feature sets were used: a) Text + Speech group, consisting of the textual features described in Section 4.1.1 and the speech features described in Section 4.1.2; b) Visual group, consisting of the features computed from motion tracking and head pose tracking outputs described in Section 4.1.3, and c) Multimodal group, a combination of the above two groups. Table 4 reports on the correlation between the human rated holistic scores and the machine predicted ones.

Table 4: Using multimodal features to predict final holistic scores on the two task types

Feature set	SVM (poly)	Glmnet
Prepared speech (Tasks B & C)		
Text + Speech	0.571	0.652
Visual	0.581	0.431
Multimodal	0.750	0.765
Impromptu speech (Tasks D & E)		
Text + Speech	0.156	0.324
Visual	0.378	0.399
Multimodal	0.525	0.592

By using the speech features from the recorded audio, transcript files, the visual features from the videos, and the motions tracked by Kinect, we find that each modality provides information for predicting overall presentation performance. Based on the text and speech features, we conclude that adding visual features improves the performance of the multimodal model. On the prepared speech tasks, the correlation increases from 0.571 to 0.750 for the SVM model and from 0.625 to 0.765 for the glmnet model. On the impromptu speech tasks, the correlation increases from 0.156 to 0.525 for the



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SVM model and from 0.324 to 0.592 for the *glmnet* model. Across the two tasks, the automated prediction results on the prepared speech are generally more accurate than on the impromptu tasks. Overall, using multimodal features, the automated scoring models achieved encouraging performance in terms of their correlation with human-rated scores.

5 DISCUSSION

In this paper, we reported a study with the goal of automatically assessing public-speaking performance using a range of multimodal cues. The achievements in this study can be summarized as follows:

First, we developed four public speaking tasks to cover two different speech types, i.e., prepared speech and impromptu speech. Seventeen subjects were recruited to perform these tasks. For data collection, we used a combination of Kinect for Windows version 1 and Brekel Pro Body software. This combination proved to be a stable setup to support our 3-D motion tracking, which lasted for about 5 minutes.

Second, we ran a rigorous human scoring process on the collected presentations. Focusing on our tasks, we tailored a particular rubric, the Public Speaking Competence Rubric (PSCR) (Schreiber et al., 2012), to our needs. Then, a series of quality control approaches were utilized in our human rating process, including pre-training, pairing expert and non-expert raters, score adjudication, etc.

Third, we extracted a set of features from speeches, transcripts, Kinect motions, and head tracking results. Regarding the features from speeches and transcripts, we mostly utilized the ample research results from the language-skill assessment area, which have not been widely utilized in the multimodal sensing field. Our motion features were mostly inspired by previous research findings in such areas as affective computing, virtual agents, etc.

Finally, we ran feature selection and machine learning tasks on a set of selected features to predict the holistic scores judged by humans. Our feature selection results on the two types of tasks showed interesting feature usage patterns that somehow reflect the tasks' differences. From the research reported in this paper, we find that the features extracted using NLP, speech processing, and multimodal sensing are helpful for building automated assessment models. More importantly, compared to the scoring model of only using speech features, adding the features from non-verbal communication, such as hand gestures and head orientation, shows improved performance. Therefore, it is very encouraging that a set of modern computational technologies, NLP, speech, and multimodal sensing, provide strong support for the goal of automatically assessing public speaking skills. With the development of the technology described in this paper, we are confident in anticipating wider usage of the technology being developed. For example, for many students, the developed technology could be used as a formative assessment tool to support their training.



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As a study in the infancy stage of this line of research, the current research has several limitations. First, the corpus used in this study is quite small — only 14 subjects with 56 presentations. Second, our data collection setup has several internal issues. For example, videos and motion traces were recorded using separate hardware/software and this made precisely synchronizing the two data streams challenging. In addition, the brightness of the smartboard made it difficult to process the video-based head pose tracking. Regarding the features, we mostly explored low/medium level features from the multimodal data streams. It is likely that some high level features, such as disfluencies across multimodal channels, gestures used for emphasizing important points, and so on, could be more meaningful for inferring presentation performance. Also, most of our features used in the final scoring models are some type of statistical value derived from the entire presentation. Although such computing provides some useful features, we anticipate that more sophisticated approaches, such as considering the temporal structure of feature contours, will be useful for more accurate modelling. It is worth noting that our current multimodal features only cover part of the full construct. For example, the existing feature-set lacks coverage of content organization.

Therefore, in our future studies, we will address the above-mentioned limitations. In particular, we will expand our corpus size, investigate extracting and utilizing some high-level non-verbal features bearing more clear semantic and social cues, and explore using more features that reflect subtle local changes. In addition, we will seek subject approval for releasing this data set to the research community.

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